

Hall Ticket Number:

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Code No. : 12121 O

VASAVI COLLEGE OF ENGINEERING (AUTONOMOUS), HYDERABAD

Accredited by NAAC with A++ Grade

B.E. II-Semester Backlog Examinations, August-2023

Engineering Mathematics-II

(Common to all Branches)

Time: 3 hours

Max. Marks: 60

Note: Answer all questions from Part-A and any FIVE from Part-B

Part-A ($10 \times 2 = 20$ Marks)

| Q. No. | Stem of the question | M | L | CO | PO |
|----------------------------------|---|---|---|----|--------|
| 1. | Define rank of a matrix. | 2 | 1 | 1 | 1,2,12 |
| 2. | If 1, 2, 3 are the eigen values of a matrix A, then find the eigen values of A^T and A^{-1} . | 2 | 2 | 1 | 1,2,12 |
| 3. | Write the differential equation governing the LR circuit. | 2 | 1 | 2 | 1,2,12 |
| 4. | Define integrating factor. | 2 | 1 | 2 | 1,2,12 |
| 5. | Solve $y'' - 2y' + y = 0$. | 2 | 2 | 3 | 1,2,12 |
| 6. | Write the differential equation governing the LCR circuit. | 2 | 1 | 3 | 1,2,12 |
| 7. | Define analytic function. | 2 | 1 | 4 | 1,2,12 |
| 8. | Write the necessary and sufficient conditions for a function to be analytic. | 2 | 1 | 4 | 1,2,12 |
| 9. | Define residue at a pole. | 2 | 1 | 5 | 1,2,12 |
| 10. | State Cauchy's integral formula. | 2 | 1 | 5 | 1,2,12 |
| Part-B (5 × 8 = 40 Marks) | | | | | |
| 11. a) | Test whether the vectors (2, 1, 1), (2, 0, -1) and (4, 2, 1) are linearly independent or dependent? | 4 | 2 | 1 | 1,2,12 |
| b) | Verify Cayley-Hamilton theorem for the matrix $\begin{pmatrix} 2 & 1 & 1 \\ 0 & 1 & 0 \\ 1 & 1 & 2 \end{pmatrix}$. | 4 | 2 | 1 | 1,2,12 |
| 12. a) | Solve $(y \cos x + \sin y + y)dx + (\sin x + x \cos y + x)dy = 0$. | 4 | 3 | 2 | 1,2,12 |
| b) | Find the general and singular solution of the equation $\rho = \log(px - y)$. | 4 | 2 | 2 | |
| 13. a) | Solve $y'' + 5y' + 6y = e^x$. | 4 | 3 | 3 | 1,2,12 |
| b) | Solve $y'' + 9y = \sin 2x$. | 4 | 3 | 3 | 1,2,12 |

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|--------|---|---|---|---|--------|
| 14. a) | Find the analytic function, whose real part is $y + e^x \cos y$. | 4 | 3 | 4 | 1,2,12 |
| b) | Find the constants a, b, c and d if $f(z) = (ax^3 - 3cxy^2 + 3dx^2 - 3by^2) + i(3x^2y - y^3 + 6xy)$ is analytic. | 4 | 3 | 4 | 1,2,12 |
| 15. a) | Evaluate $\oint_C \frac{e^z}{(z-1)^2} dz$, where C is $ z = 2$. | 4 | 3 | 5 | 1,2,12 |
| b) | Evaluate $\oint_C \left(\frac{\sin z}{z-2} + \frac{\cos z}{z-4} \right) dz$, where C is $ z = 3$. | 4 | 3 | 5 | 1,2,12 |
| 16. a) | Find the eigen values and eigen vectors of the matrix $\begin{pmatrix} 1 & 0 & 0 \\ 1 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$. | 4 | 2 | 1 | 1,2,12 |
| b) | Find the orthogonal trajectories of the family of semi cubical parabolas $ay^2 = x^3$. | 4 | 3 | 2 | 1,2,12 |
| 17. | Answer any <i>two</i> of the following: | | | | |
| a) | Solve $y'' - 6y' + 9y = e^{3x}/x^2$ by the method of variation of parameters. | 4 | 3 | 3 | 1,2,12 |
| b) | Define harmonic function. Show that $u = \frac{1}{2} \log(x^2 + y^2)$ is harmonic function. | 4 | 2 | 4 | 1,2,12 |
| c) | Find the Taylor's expansion of $f(z) = \frac{1}{(z+1)^2}$ about the point $z = 1$. | 4 | 3 | 5 | 1,2,12 |

M : Marks; L: Bloom's Taxonomy Level; CO: Course Outcome; PO: Programme Outcome

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|------|-------------------------------|-----|
| i) | Blooms Taxonomy Level – 1 | 20% |
| ii) | Blooms Taxonomy Level – 2 | 30% |
| iii) | Blooms Taxonomy Level – 3 & 4 | 50% |
